

# Statistics

## Lecture 13



Feb 19-8:47 AM

The College **claims** that **35%** of all students are fan of Online classes.  $P = .35$   $H_0$

I surveyed **175** students and **40%** of them were in favor of online classes.  $n = 175$   
 $\hat{P} = .4 \rightarrow \chi = n\hat{p} = 175(.4) = 70$

Use this survey to test the claim at  $\alpha = .1$

**$H_0: P = .35$  claim**    CV    Z    TTT     $\alpha = .1$

**$H_1: P \neq .35$  TTT**

CTS  $Z = 1.387$   
 P-value  $P = .166$  ✓

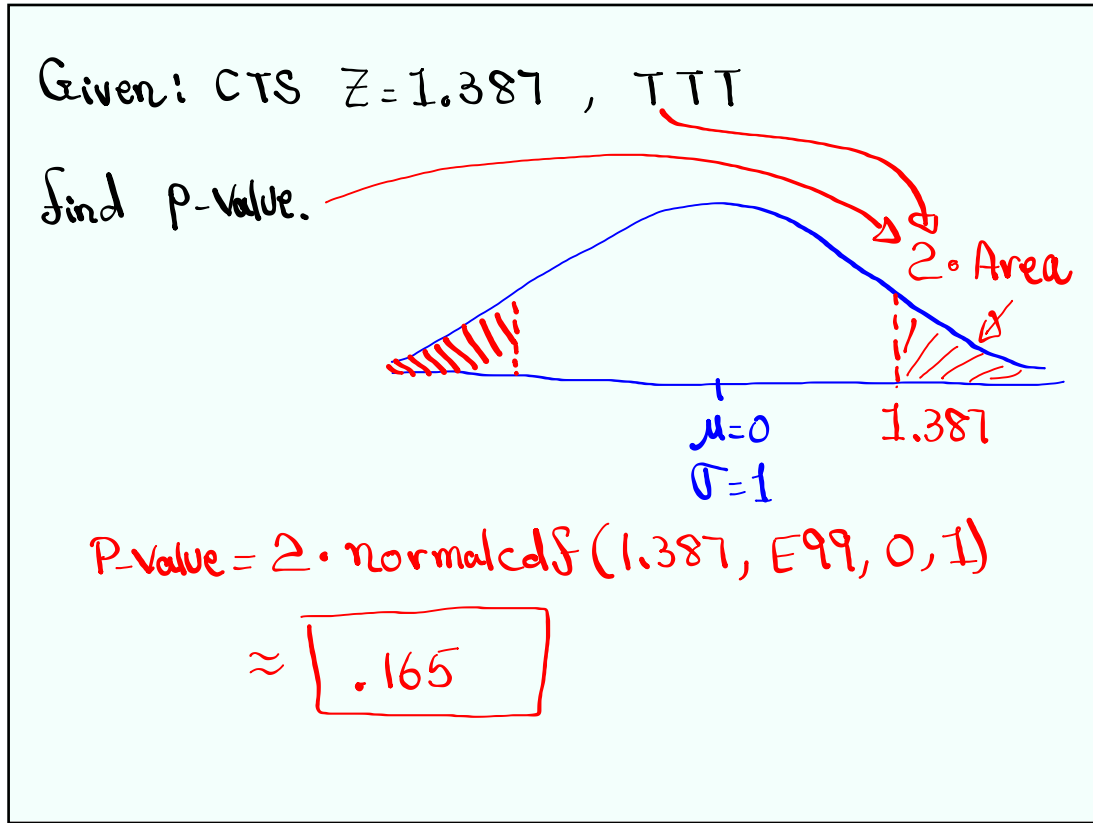
1-Prop Z Test  
 $P_0: .35$   
 $\chi: 70$   
 $n: 175$   
 Prop  $\neq P_0$   $H_1$

$Z = \text{invNorm}(.95, 0, 1)$

CTS is in NCR  $\Rightarrow H_0$  valid  
 P-value  $> \alpha \Rightarrow H_1$  invalid

valid claim  
 Fail-to-  
 Reject

May 22-8:06 AM



May 22-8:20 AM

The College claims the mean age of all students is at most 32.5 yrs.  $\mu \leq 32.5$   
 $\leftarrow H_0$

I randomly selected 40 students, their mean age was 36.8 yrs.  
 $n=40$   $\bar{x}=36.8$

Use this sample to test the claim assuming standard deviation of ages of all students is 8.8 yrs.  
 $\sigma=8.8$

$H_0: \mu \leq 32.5$  claim  $\sigma$  known Case I  
 $H_1: \mu > 32.5$  RTT CV Z RTT  $\alpha=.05$

CTS  $Z = 3.090$   
 P-value  $P = 9.995 \times 10^{-4}$

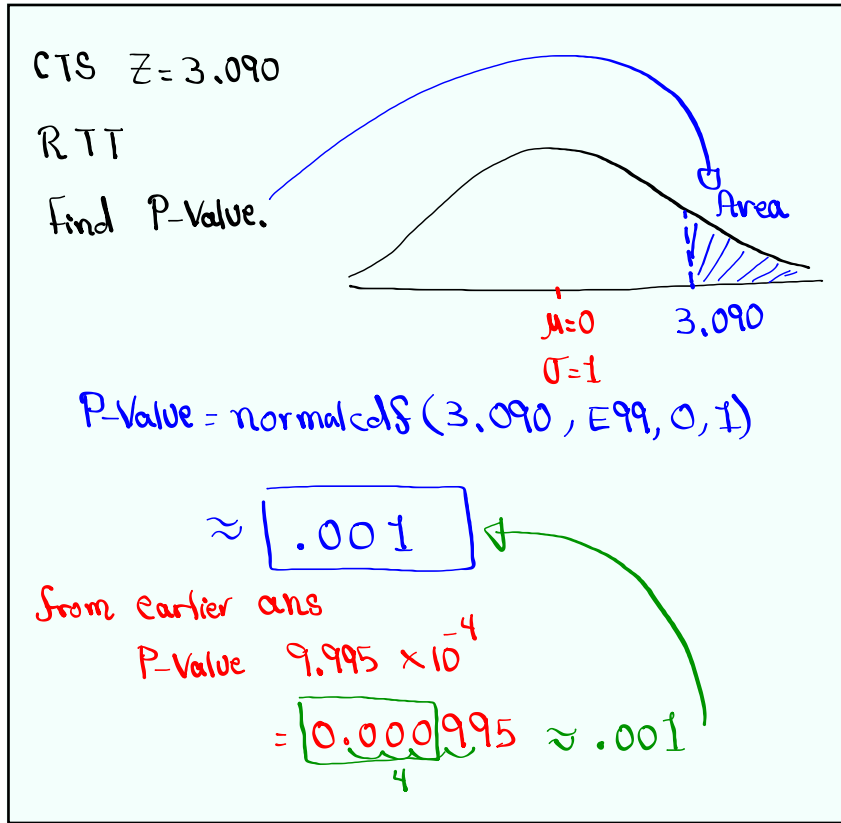
Z-Test  
 inpt: **Stats**  
 $\mu_0: 32.5$   
 $\sigma: 8.8$   
 $\bar{x}: 36.8$   
 $n: 40$   
 $\mu > \mu_0$   $H_1$

$\mu = 0$   $\sigma = 1$   $1.645$

CV  $Z = \text{invNorm}(.95, 0, 1)$

CTS is in CR  $H_0$  invalid  
 $P\text{-value} \leq \alpha \Rightarrow H_1$  valid  
 Invalid claim  
**Reject**

May 22-8:24 AM



May 22-8:38 AM

The College claims the mean score on all math exams is below 85.  $\mu < 85$   
 $\leftarrow H_1$

I took 10 exams and here are the scores.

|    |    |    |     |    |
|----|----|----|-----|----|
| 75 | 82 | 86 | 90  | 70 |
| 68 | 88 | 85 | 100 | 55 |

$\bar{x} \approx 80$   
 $S \approx 13$   $n = 10$   
 $\alpha = 0.05$

use this sample to test the claim.

$H_0: \mu \geq 85$   $\sigma$  Unknown Case II  
 $H_1: \mu < 85$  claim, LTT cv t LTT  $\alpha = 0.05$   
 $df = n - 1 = 9$

CTS  $t = -1.216$   
 P-value  $P = .127$

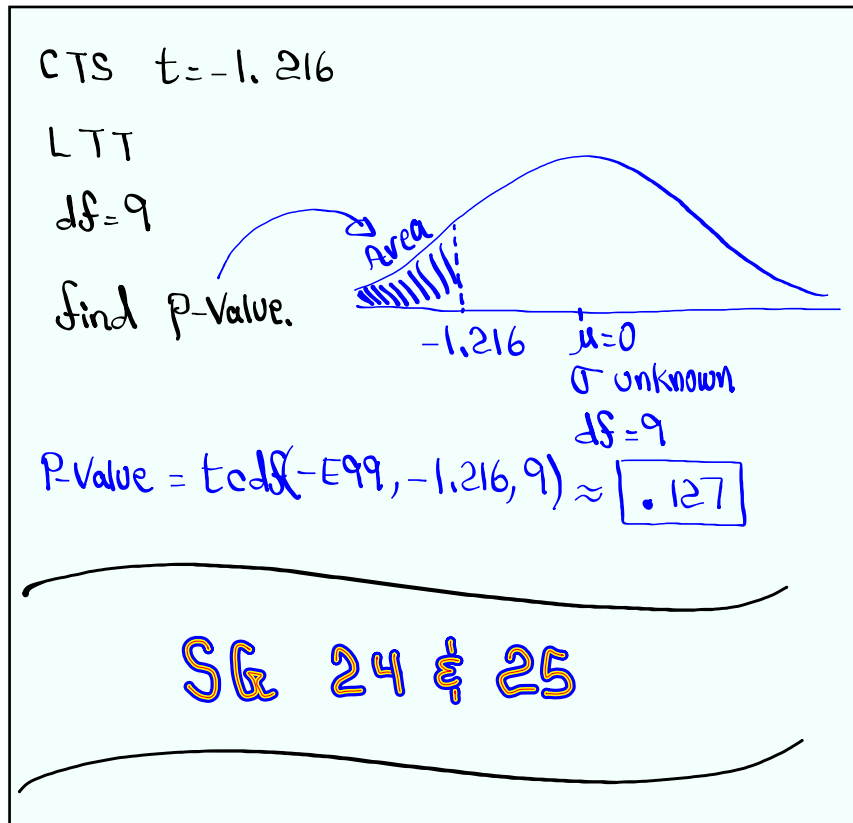
T-Test  
 inpt: Stats  
 $\mu_0 = 85$   
 $\bar{x} = 80$   
 $S = 13$   
 $n = 10$   
 $\mu < \mu_0 H_1$

$t = \text{invT}(0.05, 9)$   
 CTS is in NCR  $\Rightarrow H_0$  Valid  
 $P\text{-value} > \alpha \Rightarrow H_1$  Invalid

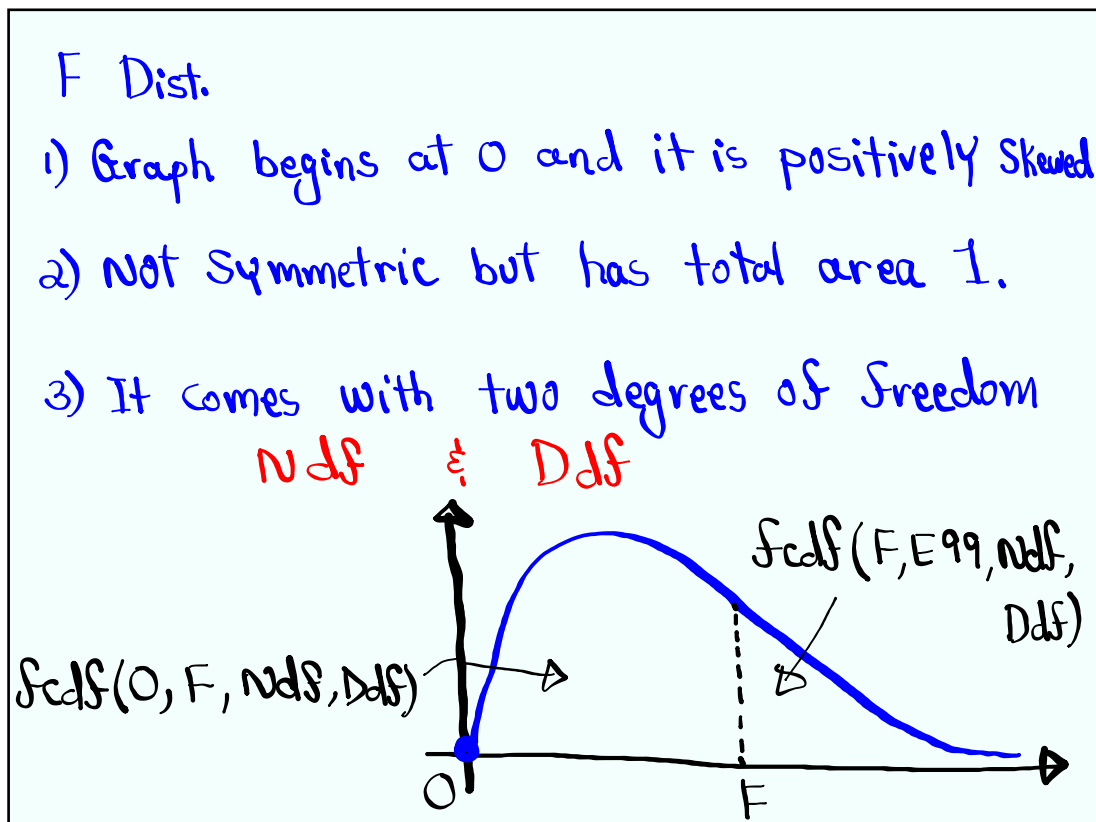
what  $\alpha$  values will reverse the conclusion?  
 Choose  $.13, .14, .15, \dots$   
 we need  $P\text{-value} \leq \alpha$

Invalid claim  
 Reject

May 22-8:45 AM

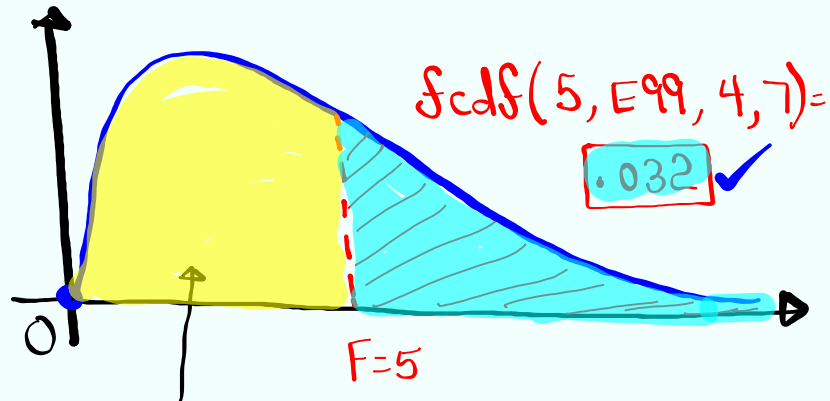


May 22-9:01 AM



May 22-9:24 AM

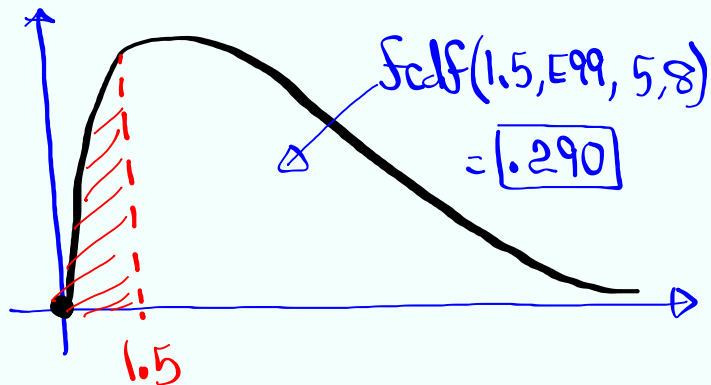
find  $P(F > 5)$  with  $Ndf=4 \hat{=} Ddf=7$ .



$$P(F < 5) = f_{cdf}(0, 5, 4, 7) =$$
.968 ✓

May 22-9:29 AM

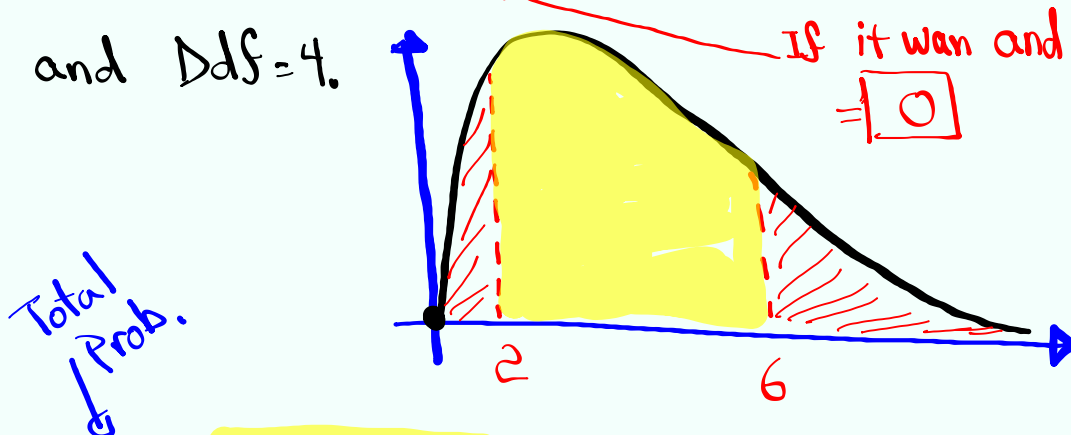
find  $P(F < 1.5)$  with  $Ndf=5 \hat{=} Ddf=8$ .



$$= f_{cdf}(0, 1.5, 5, 8) =$$
.710

May 22-9:33 AM

Find  $P(F < 2 \text{ or } F > 6)$  with  $Ndf=6$ ,  
and  $Ddf=4$ .



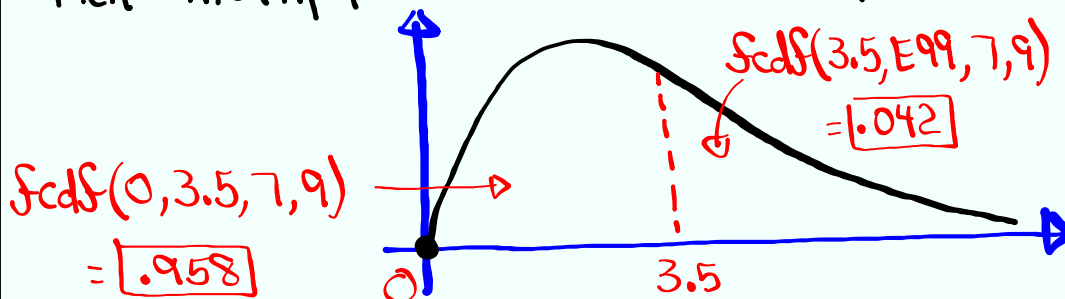
$$= 1 - P(2 < F < 6) = 1 - Fcdf(2, 6, 6, 4)$$

$$= \boxed{.791}$$

May 22-9:36 AM

Find the area on each side of  $F=3.5$   
with  $Ndf=7$  &  $Ddf=9$ .

then multiply the smaller area by 2.



$$2 \cdot \text{Smaller area} = 2(.042) = \boxed{.084}$$

May 22-9:40 AM

Comparing two Population Standard deviations:

|                               |                               |                               |
|-------------------------------|-------------------------------|-------------------------------|
| $H_0: \sigma_1 = \sigma_2$    | $H_0: \sigma_1 \leq \sigma_2$ | $H_0: \sigma_1 \geq \sigma_2$ |
| $H_1: \sigma_1 \neq \sigma_2$ | $H_1: \sigma_1 > \sigma_2$    | $H_1: \sigma_1 < \sigma_2$    |
| TTT                           | RTT                           | LTT                           |

| Group 1     | Group 2 |
|-------------|---------|
| $n_1 =$     | $n_2 =$ |
| $s_1 =$     | $s_2 =$ |
| $S_1 > S_2$ |         |

CTS  $F = \frac{S_1^2}{S_2^2}$   
 Ndf =  $n_1 - 1$ , Ddf =  $n_2 - 1$

P-value  
Area = P-value  
RTT  
CTS F  
Area = P-value  
LTT  
For TTT  
Multiply the Smaller area by 2.

P-Value Method

$P\text{-Value} > \alpha$   
 $H_0$  valid &  $H_1$  invalid

$P\text{-Value} \leq \alpha$   
 $H_0$  invalid &  $H_1$  valid

May 22-9:46 AM

Use the chart below to test the claim that  $\sigma_1 = \sigma_2$ .

|           |            |                                   |
|-----------|------------|-----------------------------------|
| Group 1   | Group 2    | $H_0: \sigma_1 = \sigma_2$ claim  |
| $n_1 = 6$ | $n_2 = 10$ | $H_1: \sigma_1 \neq \sigma_2$ TTT |
| $s_1 = 8$ | $s_2 = 4$  | No $\alpha \rightarrow .05$       |
|           |            | $S_1 > S_2 \checkmark$            |

CTS  $F = \frac{S_1^2}{S_2^2} = \frac{8^2}{4^2} = 4$   
 Ndf =  $n_1 - 1 = 5$   
 Ddf =  $n_2 - 1 = 9$

Scdf(4, 5, 9) = .035  
 Scdf(0, 4, 5, 9) = .965  
 P-value = 2 \* Smaller area =  $2(.035) = .07$

$P\text{-Value} > \alpha$

$\Rightarrow H_0$  valid  $\rightarrow$  valid claim  
 $H_1$  invalid FTR the claim

Suggest  $\alpha$  values to reverse the conclusion.  
 we need  $P\text{-Value} \leq \alpha$   $\rightarrow .07 \leq \alpha$   
 choose  $\alpha$  to be .08, .09, .10, ...

May 22-9:56 AM

|           |            |                                    |
|-----------|------------|------------------------------------|
| Group 1   | Group 2    |                                    |
| $n_1 = 6$ | $n_2 = 10$ | <b>STAT</b>                        |
| $S_1 = 8$ | $S_2 = 4$  | <b>TESTS</b>                       |
|           |            | <b>2-Samp F Test</b>               |
|           |            | Inpt: <b>Stats</b>                 |
|           |            | $S_1 = 8$                          |
|           |            | $n_1 = 6$                          |
|           |            | $S_2 = 4$                          |
|           |            | $n_2 = 10$                         |
|           |            | $\sigma_1 \neq \sigma_2 \quad H_1$ |

CTS  $F = 4$   
P-Value  $P = .069$

May 22-10:06 AM

Standard dev. of 8 exams by Female Students was 9.  
 $n=8 \quad S=9$

Standard dev. of 10 exams by male Students was 6.  
 $n=10 \quad S=6$

Test the claim at  $\alpha = .02$  that there is a difference between two POP. standard deviations.

|             |            |  |
|-------------|------------|--|
| Females     | Males      | $H_0: \sigma_1 = \sigma_2$                             |
| $n_1 = 8$   | $n_2 = 10$ | $H_1: \sigma_1 \neq \sigma_2$ claim TTT                |
| $S_1 = 9$   | $S_2 = 6$  | CTS $F = \frac{S_1^2}{S_2^2} = \frac{9^2}{6^2} = 2.25$ |
| $S_1 > S_2$ |            | ndf = 7, Ddf = 9                                       |

$P\text{-Value} > \alpha$   
 $.256 > .02$   
 $H_0$  valid &  $H_1$  invalid  
Invalid claim  $\rightarrow$  **Reject**

Use 2-Samp F Test, Sind  
CTS  $F = 2.25$   
P-Value  $P = .256$

$Scdf(2.25, 7, 9) = .128$   
 $Scdf(0, 2.25, 7, 9) = .972$   
 $P\text{-Value} = 2(.128) = .256$

May 22-10:09 AM

Stand. dev. of ages of 8 Female nurses was 10 yrs.  $n=8$   $S=10$

Stand. dev. of ages of 8 male nurses was 4 yrs.  $n=8$   $S=4$

Use  $\alpha=.1$  to test the claim that Standard dev. of ages of all Female nurses is greater than the standard dev. of ages of all male nurses.

$\sigma_1 > \sigma_2$   $H_1$

| Females  | Males   |
|----------|---------|
| $n_1=8$  | $n_2=8$ |
| $S_1=10$ | $S_2=4$ |

$S_1 > S_2$

$H_0: \sigma_1 \leq \sigma_2$

$H_1: \sigma_1 > \sigma_2$  claim RTT

2-Samp F Test

CTS  $F=6.25$

P-Value  $P=.014$

$P\text{-Value} < \alpha$

$.014 < .1$

$H_0$  invalid

$H_1$  valid Valid claim  $\rightarrow$  FTR the claim

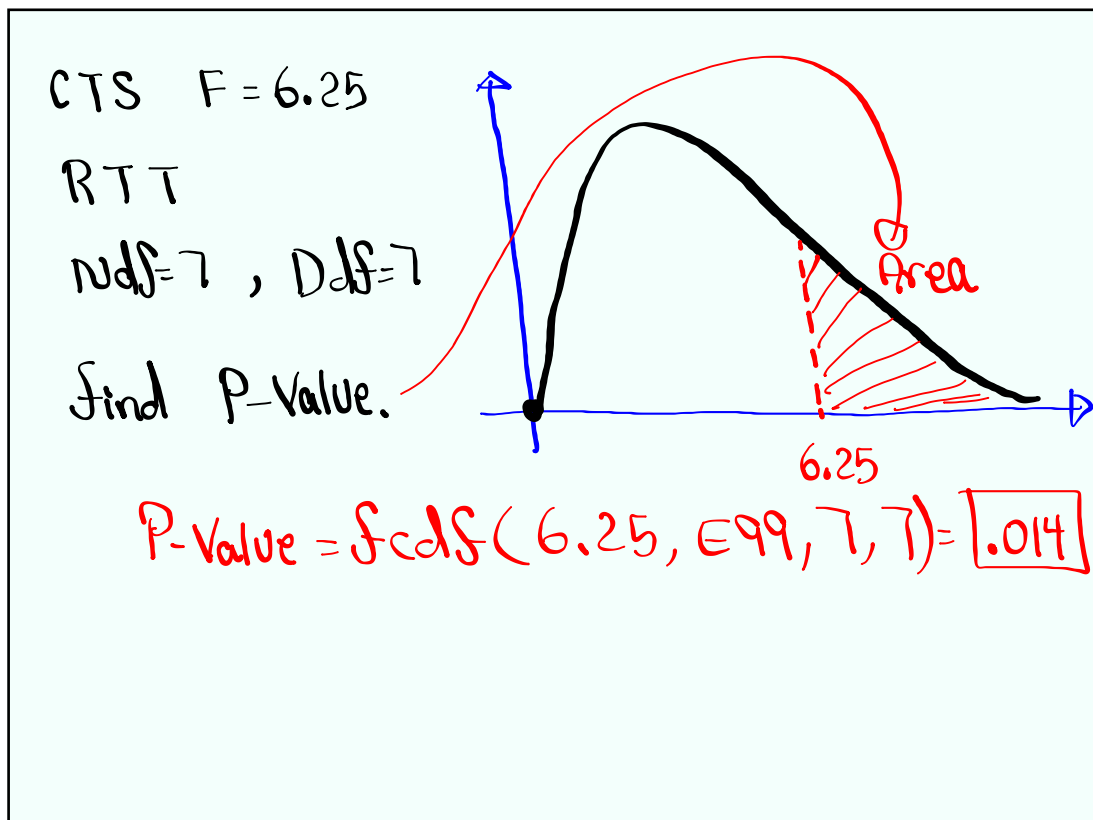
Suggest a value for  $\alpha$  to reject the claim.

we need  $P\text{-Value} > \alpha$

$.014 > \alpha$

choose  $\alpha=.01$

May 22-10:23 AM



May 22-10:34 AM